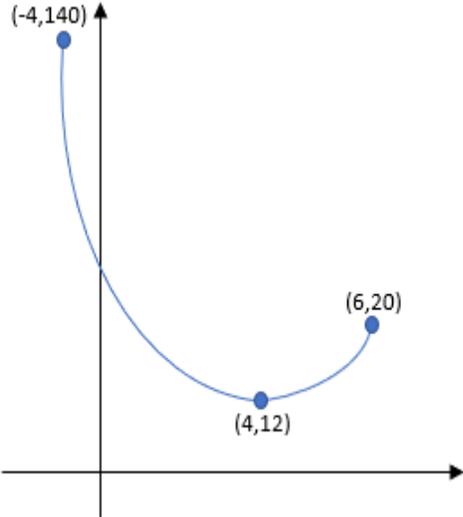
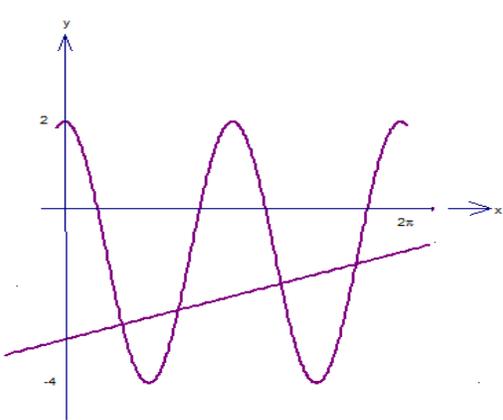


**Peraturan Pemarkahan Ujian Diagnostik Tingkatan 5 Matematik Tambahan  
(Kertas 2 / 2021)**

| No | Solutions and marking Scheme   | Sub marks                                    | Total Marks     |
|----|--|--|-----------------|
| 1  | <p>Murid/Students: <math>x</math><br/> Dewasa/Adults: <math>y</math><br/> Warga emas/Senior citizens: <math>z</math></p> $\left. \begin{array}{l} x = 2y + 2z \dots\dots\dots (1) \\ x + y + z = 120 \dots\dots\dots (2) \\ 5x + 10y + 7.5z = 775 \dots\dots\dots (3) \end{array} \right\} \begin{array}{ c } \hline \text{Either} \\ \hline \text{one} \\ \hline \end{array}$ <p>Eliminate one of the unknown by substitution or elimination method</p> <p>Substitute (1) into (2)<br/> <math>3y + 3z = 120</math><br/> <math>y + z = 40 \dots\dots\dots (4)</math> } OR other valid method</p> <p>Substitute (1) into (3)<br/> <math>5(2y + 2z) + 10y + 7.5z = 775</math><br/> <math>20y + 17.5z = 775 \dots\dots\dots (5)</math> } <span style="border: 1px solid black; padding: 2px;">Either one</span></p> <p><math>[(4) \times 20] - (5)</math><br/> <math>20y + 20z = 800</math><br/> <math>20y + 17.5z = 775</math><br/> <math>2.5z = 250</math><br/> <math>z = 10</math> (Warga emas/Senior citizens)</p> <p><math>y = 30</math> (Dewasa/Adults)<br/> <math>x = 80</math> (Murid/Students)</p> | <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> | <p><b>5</b></p> |

|       |   |   |          |          |
|-------|---|---|----------|----------|
| 2 (a) | $h=2t$<br>$k=\frac{3}{2}t^2$  | 1<br>1  |          |          |
| (b)   |    | Shape $\cup$ 1<br>Min. point(4,12) 1<br>(-4,140) and (6,20) 1 | <b>8</b> |          |
| (c)   | $2x^2-16x+44-n=0$<br>$(-16)^2-4(2)(44-n)\geq 0$<br>$n\geq 12$   | 1<br>1<br>1   |          |          |
| 3 (a) | (i) $m_{PR} = \frac{1}{4}$<br>$y - 4 = \frac{1}{4}(x - (-1))$<br>$y = \frac{1}{4}x + \frac{17}{4}$ or equivalent<br><br>(ii) $k = 11$<br>$\sqrt{[11 - (-1)]^2 + (7 - 4)^2}$<br>12.37 or $\sqrt{153}$<br><br>$T = \left( \frac{3(11) + 1(-1)}{3+1}, \frac{3(7) + 1(4)}{3+1} \right)$<br>$= \left( 8, \frac{25}{4} \right)$ | 1<br>1<br>1<br>1<br>1<br>1                                    |          | <b>8</b> |
| (b)   |   | 1   |          |          |

|                                    |  |   |                 |
|------------------------------------|--|---|-----------------|
| <p>4 (a)</p> <p>(b)</p> <p>(c)</p> | $-3 = -3(-1)^2 - 2p(-1) + 4$ $p = -2$ <p><math>(-1, 2)</math><br/> <math>y - 2 = -3(x + 1)</math><br/> <math>y = -3x - 1</math> or equivalent</p> $-3x^2 + 4x + 4 = 0$ $(3x + 2)(x - 2) = 0$ $x = -\frac{2}{3}, 2$   | <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>   | <p><b>8</b></p> |
| <p>5 (a)</p> <p>(b)</p>            | $\frac{1}{2}(9^2)\left(\frac{\pi}{3}\right) \text{ or } \frac{1}{2}(9^2)(\sin 60^\circ)$ $\frac{1}{2}(9^2)\left(\frac{\pi}{3}\right) - \frac{1}{2}(9^2)(\sin 60^\circ)$ $7.343 \text{ cm}^2$ <p><math>AC = \sqrt{9^2 + 9^2 - 2(9)(9)\cos 120^\circ}</math> OR other valid method</p> $\text{Arc AB} + \text{Arc DC} = 9\left(\frac{2}{3}\pi\right) - 9\left(\frac{1}{3}\pi\right)$ $\text{Perimeter} = (9\sqrt{3} + 9 + 3\pi)$ | <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1,1</p> <p>1</p> | <p><b>7</b></p> |
| <p>6 (a)</p> <p>(b)</p>            | <p><i>LHS</i></p> $= 2\cos^2 x + (\tan^2 x - \sec^2 x) \text{ OR other valid method}$ $= 2\cos^2 x - 1$ $= \cos 2x$   | <p>1</p> <p>1</p>                                       | <p><b>7</b></p> |

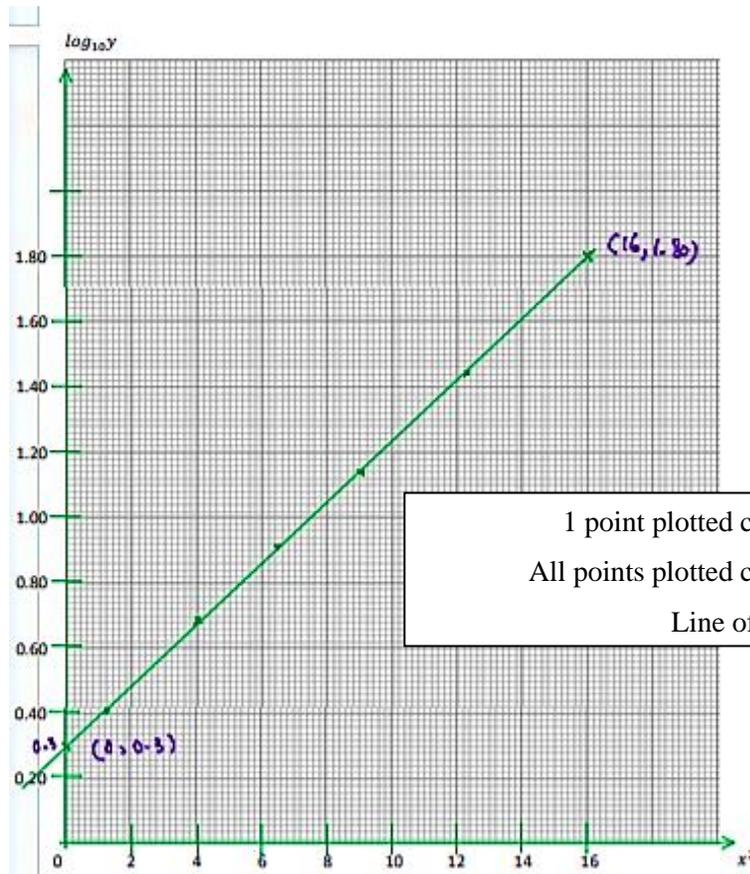
|       |   |                               |   |
|-------|---|-------------------------------|---|
|       | Shape of cosine<br>Amplitude ( $y_{min} = -4, y_{max} = 2$ )<br>Number of cycles in $0 \leq x \leq 2\pi \text{ rad} = 2$<br><br>$3\cos^2 x - 1 = \frac{x}{\pi} - 3$ or $y = \frac{x}{\pi} - 3$<br><br>Number of solutions = 4                       | 1<br>1<br>1<br><br>1<br><br>1 |   |
| 7 (a) | $\frac{1}{\log_m mn} + \frac{1}{\log_m mn}$ OR change correctly base of $\log_m mn$ or $\log_n mn$<br>$\frac{1}{\log_m m} + \frac{1}{\log_m n}$<br><br>$\log_{mn} m + \log_{mn} n$<br>$\log_{mn} mn = 1$<br><br>$2x - 1 = 6^1$<br>$x = \frac{7}{2}$ | 1<br><br><br>1<br><br>1<br>1  | 7 |
| (b)   | $5^{2x} - 5(5^x) - 50 = 0$<br>$(5^x + 5)(5^x - 10) = 0$<br>$x = 1.431$  | 1<br>1<br>1                   |   |
|       |   |                               |   |

8 (a)

|               |      |      |      |      |       |       |
|---------------|------|------|------|------|-------|-------|
| $x^2$         | 1.00 | 4.00 | 6.25 | 9.00 | 12.25 | 16.00 |
| $\log_{10} y$ | 0.40 | 0.68 | 0.91 | 1.15 | 1.44  | 1.80  |

1  
1

**10**



1 point plotted correctly  
All points plotted correctly  
Line of best fit

1  
1  
1

(b)

$$\log_{10} y = -\log_{10} n x^2 + \log_{10} k$$

1

$$\log_{10} k = *c$$

1

$$\text{terima } 1.95 \leq k \leq 2.05$$

1

$$-\log_{10} n = *m$$

1

$$\text{terima } 0.80 \leq n \leq 0.82$$

1

|         |  |                        |           |
|---------|--|------------------------|-----------|
| 9 (a) i | $\overrightarrow{AM} = \frac{1}{2}(\overrightarrow{AO} + \overrightarrow{OB})$ $= -\frac{1}{2} \mathbf{a} + \frac{1}{2} \mathbf{b}$  | 1<br>1                 | <b>10</b> |
| (ii)    | $\overrightarrow{AP} = (\overrightarrow{AO} + \overrightarrow{OP}) \text{ or } \overrightarrow{OM} = (\overrightarrow{OA} + \overrightarrow{AM})$  | 1<br>1                 |           |
| (iii)   | $\overrightarrow{OM} = \frac{1}{2} \mathbf{a} + \frac{1}{2} \mathbf{b}$  | 1                      |           |
| (b)     | $\overrightarrow{OQ} = \frac{1}{2}h \mathbf{a} + \frac{1}{2}h \mathbf{b} \quad \text{or} \quad \overrightarrow{OQ} = (1 - k)\mathbf{a} + \frac{1}{3}k \mathbf{b}$ $\text{or } \overrightarrow{AQ} = -k\mathbf{a} + \frac{1}{3} \mathbf{b}$ $\frac{1}{2}h = 1 - k \text{ or } \frac{1}{2}h = \frac{1}{3}k$ <p>solve simultaneous equation to find <math>h</math> or <math>k</math></p> $h = \frac{1}{2}, k = \frac{3}{4}$ | 1<br><br>1<br>1<br>1,1 |           |
| 10 (a)  | $\frac{dy}{dx} = \frac{1}{2}(x - 5)^{-\frac{1}{2}}$ $m_2 = -2$ $y - 1 = -2(x - 6)$ $y = -2x + 13$  | 1<br>1<br>1<br>1       | <b>10</b> |
| (b)     | $= \left[ \frac{y^3}{3} + 5y \right]_0^1 - \frac{1}{2}(1)(6 + 4) \text{ or other valid method}$ $= \frac{1}{3}$  | 1, 1<br>1              |           |
| (c)     | $\text{Volume} = \pi \int_5^6 (x - 5) dx$ $= \pi \left[ \frac{x}{2} - 5x \right]_5^6$ $= 0.5 \pi$  | 1<br>1<br>1            |           |

|         |   |   |           |
|---------|---|---|-----------|
| 11 (a)  | $12C_r \left(\frac{3}{5}\right)^r \left(\frac{2}{5}\right)^{n-r}$ $P(X=10) + P(X=11) + P(X=12)$ $12C_{10} \left(\frac{3}{5}\right)^{10} \left(\frac{2}{5}\right)^2 + 12C_{11} \left(\frac{3}{5}\right)^{11} \left(\frac{2}{5}\right)^1 + 12C_{12} \left(\frac{3}{5}\right)^{12} \left(\frac{2}{5}\right)^0$ $0.08344$   | 1<br>1<br>1<br>1                          |           |
| (b) (i) | $P(X \geq 40) = P\left(Z \geq \frac{40 - 48}{16}\right)$ $= P(Z \geq -0.5)$ $= 1 - P(Z \leq -0.5)$ $= 0.6915$ <p>% of students who passed = 69.15</p>   | 1<br>1<br>1                               | <b>10</b> |
| (ii)    | $z = 1.751$ $\frac{X-48}{16} = 1.751$ $X = 76.02$   | 1<br>1<br>1                               |           |
| 12 (a)  | <p>(a) <math>\angle PRQ = 180^\circ - 50^\circ - 48^\circ</math><br/><math>= 82^\circ</math></p> <p>(i) <math>\frac{55}{\sin 48^\circ} = \frac{PQ}{\sin 82^\circ}</math><br/><math>PQ = 73.29 \text{ m}</math></p> <p>(ii) <math>25^2 = 70^2 + 55^2 - 2(70)(55) \cos \angle RPS</math><br/><math>\angle RPS = 18.54^\circ</math></p> <p>(iii) <math>\frac{1}{2} (55)(73.29) \sin 50^\circ</math><br/><math>1543.94</math></p> <p>(b) <math>\angle PRX = 50^\circ</math> or <math>\angle PXR = 80^\circ</math><br/><math>\cos 50^\circ = \frac{27.5}{PX}</math> OR <math>\frac{PX}{\sin 50^\circ} = \frac{55}{\sin 80^\circ}</math><br/><math>42.78</math></p> | 1<br>1<br>1<br>1<br>1<br>1<br>1<br>1<br>1 | <b>10</b> |

|    |     |   |                  |    |
|----|-----|---|------------------|----|
| 13 | (a) | $\frac{96}{80} \times 100 = x \quad \text{or} \quad \frac{60}{y} \times 100 = 125 \quad \text{or} \quad \frac{z}{50} \times 100 = 150$ $x = 120$ $y = 48$ $z = 75$  | 1                | 10 |
|    | (b) | i) $\frac{120(3)+125(h)+150(5)}{3+h+5} = 136$ $125h + 1110 = 136(8 + h)$ $125h + 1110 = 1088 + 136h$ $h = 2$<br>ii) $\frac{x}{16000} \times 100 = 136$ $x = \text{RM}21760.00$  | 1<br>1<br>1      |    |
|    | (c) | $I_{2006/2000} = \frac{120 \times 100}{100}$ $= 132$  | 1<br>1           |    |
| 14 | (a) | $v = 24$  | 1                | 10 |
|    | (b) | $2t - 10 = 0$<br>$5^2 - 10(5) + 24$<br>$= -1$   | 1<br>1<br>1      |    |
|    | (c) | $t^2 - 10t + 24 < 0$<br>$(t - 6)(t - 4) < 0$<br>$4 < t < 6$   | 1<br>1           |    |
|    | (d) | $S = \int t^2 - 10t + 24 \, dt = \frac{t^3}{3} - 5t^2 + 24t + c$ Ganti $t = 4$ , $s = 37\frac{1}{3}$ atau $t = 5$ , $s = 36\frac{2}{3}$<br>Jumlah jarak = $37\frac{1}{3} + (37\frac{1}{3} - 36\frac{2}{3})$<br>$= 38$ | 1<br>1<br>1<br>1 |    |

|        |   |  |           |   |
|--------|---|--|-----------|---|
| 15 (a) | I: $x + y \leq 80$  | 1  | <b>10</b> |   |
|        | II: $y \leq 4x$   | 1  |           |   |
|        | III: $y - x \geq 10$  | 1  |           |   |
|        | (b)   | Draw correctly at least one straight line from the                       |           | 1 |
|        |   | <b>*inequalities</b> which involves <b>x</b> and <b>y</b> .              |           |   |
|        |   | Draw correctly all the three straight lines.<br>Note: Accept dotted line |           | 1 |
|        | Region shaded correctly.  | 1  |           |   |
| (c)    | i) $30 \leq y \leq 60$  | 1, 1   |           |   |
|        | ii) maximum point <b>(16,64)</b>                                      |  |           |   |
|        | Use <b><math>60x + 70y</math></b> for any point in the <b>*region</b> | 1  |           |   |
|        | the maximum total fees = RM5440                                       | 1  |           |   |

# Lampiran 1

